

# Midterm format



- Date: 10/09/2003 from 11:00am – 12:20 pm
- Location: disclosed in class
- Credits: 35% of overall grade
- Approx. 4 problems, several questions in each.
- Material: everything so far.
- **Not** a multiple choice exam
- No books (or other material) are allowed.
- Duration will be 1:20 hours.
- Academic Integrity code: see class main page.

## Last time: Logic and Reasoning

- Knowledge Base (KB): contains a set of sentences expressed using a **knowledge representation language**
  - TELL: operator to add a sentence to the KB
  - ASK: to query the KB
- Logics are KRLs where conclusions can be drawn
  - Syntax
  - Semantics
- Entailment:  $KB \models a$  iff  $a$  is true in all worlds where KB is true
- Inference:  $KB \vdash_i a$  = sentence  $a$  can be derived from KB using procedure  $i$ 
  - Sound: whenever  $KB \vdash_i a$  then  $KB \models a$  is true
  - Complete: whenever  $KB \models a$  then  $KB \vdash_i a$

## Last Time: Syntax of propositional logic

Propositional logic is the simplest logic—illustrates basic

The proposition symbols  $P_1, P_2$  etc are sentences

If  $S$  is a sentence,  $\neg S$  is a sentence

If  $S_1$  and  $S_2$  is a sentence,  $S_1 \wedge S_2$  is a sentence

If  $S_1$  and  $S_2$  is a sentence,  $S_1 \vee S_2$  is a sentence

If  $S_1$  and  $S_2$  is a sentence,  $S_1 \Rightarrow S_2$  is a sentence

If  $S_1$  and  $S_2$  is a sentence,  $S_1 \Leftrightarrow S_2$  is a sentence

# Last Time: Semantics of Propositional logic

Each model specifies true/false for each proposition symbol

E.g.  $A \quad B \quad C$   
*True True False*

Rules for evaluating truth with respect to a model  $m$ :

$\neg S$	is true iff	$S$	is false
$S_1 \wedge S_2$	is true iff	$S_1$	is true <u>and</u> $S_2$ is true
$S_1 \vee S_2$	is true iff	$S_1$	is true <u>or</u> $S_2$ is true
$S_1 \Rightarrow S_2$	is true iff	$S_1$	is false <u>or</u> $S_2$ is true
	i.e., is false iff	$S_1$	is true <u>and</u> $S_2$ is false
$S_1 \Leftrightarrow S_2$	is true iff	$S_1 \Rightarrow S_2$	is true <u>and</u> $S_2 \Rightarrow S_1$ is true

# Last Time: Inference rules for propositional logic

- ◇ **Modus Ponens** or **Implication-Elimination**: (From an implication and the premise of the implication, you can infer the conclusion.)

$$\frac{\alpha \Rightarrow \beta, \quad \alpha}{\beta}$$

- ◇ **And-Elimination**: (From a conjunction, you can infer any of the conjuncts.)

$$\frac{\alpha_1 \wedge \alpha_2 \wedge \dots \wedge \alpha_n}{\alpha_i}$$

- ◇ **And-Introduction**: (From a list of sentences, you can infer their conjunction.)

$$\frac{\alpha_1, \alpha_2, \dots, \alpha_n}{\alpha_1 \wedge \alpha_2 \wedge \dots \wedge \alpha_n}$$

- ◇ **Or-Introduction**: (From a sentence, you can infer its disjunction with anything else at all.)

$$\frac{\alpha_i}{\alpha_1 \vee \alpha_2 \vee \dots \vee \alpha_n}$$

- ◇ **Double-Negation Elimination**: (From a doubly negated sentence, you can infer a positive sentence.)

$$\frac{\neg\neg\alpha}{\alpha}$$

- ◇ **Unit Resolution**: (From a disjunction, if one of the disjuncts is false, then you can infer the other one is true.)

$$\frac{\alpha \vee \beta, \quad \neg\beta}{\alpha}$$

- ◇ **Resolution**: (This is the most difficult. Because  $\beta$  cannot be both true and false, one of the other disjuncts must be true in one of the premises. Or equivalently, implication is transitive.)

$$\frac{\alpha \vee \beta, \quad \neg\beta \vee \gamma}{\alpha \vee \gamma} \quad \text{or equivalently} \quad \frac{\neg\alpha \Rightarrow \beta, \quad \beta \Rightarrow \gamma}{\neg\alpha \Rightarrow \gamma}$$

## This time



- **First-order logic**
  - Syntax
  - Semantics
  - Wumpus world example
- **Ontology** (ont = 'to be'; logica = 'word'): kinds of things one can talk about in the language

## Why first-order logic?



- We saw that propositional logic is limited because it only makes the ontological commitment that the world consists of **facts**.
- Difficult to represent even simple worlds like the Wumpus world;

e.g.,

“don't go forward if the Wumpus is in front of you”  
takes 64 rules

# First-order logic (FOL)



- Ontological commitments:
  - **Objects:** wheel, door, body, engine, seat, car, passenger, driver
  - **Relations:** Inside(car, passenger), Beside(driver, passenger)
  - **Functions:** ColorOf(car)
  - **Properties:** Color(car), IsOpen(door), IsOn(engine)
- Functions are relations with single value for each object



# Semantics



there is a correspondence between

- functions, which return values
- predicates, which are true or false

Function:  $\text{father\_of}(\text{Mary}) = \text{Bill}$

Predicate:  $\text{father\_of}(\text{Mary}, \text{Bill})$

## Examples:



- “One plus two equals three”

Objects:

Relations:

Properties:

Functions:

- “Squares neighboring the Wumpus are smelly”

Objects:

Relations:

Properties:

Functions:

## Examples:



- “One plus two equals three”

Objects: one, two, three, one plus two

Relations: equals

Properties: --

Functions: plus (“one plus two” is the name of the object obtained by applying function plus to one and two; three is another name for this object)

- “Squares neighboring the Wumpus are smelly”

Objects: Wumpus, square

Relations: neighboring

Properties: smelly

Functions: --

## FOL: Syntax of basic elements

- **Constant symbols:** 1, 5, A, B, USC, JPL, Alex, Manos, ...
- **Predicate symbols:**  $>$ , Friend, Student, Colleague, ...
- **Function symbols:** +, sqrt, SchoolOf, TeacherOf, ClassOf, ...
- **Variables:**  $x, y, z, next, first, last, \dots$
- **Connectives:**  $\wedge, \vee, \Rightarrow, \Leftrightarrow$
- **Quantifiers:**  $\forall, \exists$
- **Equality:** =

# Syntax of Predicate Logic



- Symbol set
  - **constants**
  - **Boolean connectives**
  - variables
  - functions
  - predicates (relations)
  - quantifiers

# Syntax of Predicate Logic



- Terms: a reference to an object
  - variables,
  - constants,
  - functional expressions (can be arguments to predicates)
- Examples:
  - `first([a,b,c])`, `sq_root(9)`, `sq_root(n)`, `tail([a,b,c])`

# Syntax of Predicate Logic



- Sentences: make claims about objects
  - (Well-formed formulas, (wffs))
- **Atomic Sentences** (predicate expressions):
  - loves(John,Mary), brother\_of(John,Ted)
- **Complex Sentences** (Atomic Sentences connected by booleans):
  - loves(John,Mary)
  - brother\_of(John,Ted)
  - teases(Ted, John)

# Examples of Terms: Constants, Variables and Functions

- Constants: object constants refer to individuals
  - Alan, Sam, R225, R216
- Variables
  - PersonX, PersonY, RoomS, RoomT
- Functions
  - father\_of(PersonX)
  - product\_of(Number1, Number2)



# Examples of Predicates and Quantifiers



- Predicates
  - `in(Alan,R225)`
  - `partOf(R225,Pender)`
  - `fatherOf(PersonX,PersonY)`
- Quantifiers
  - All dogs are mammals.
  - Some birds can't fly.
  - 3 birds can't fly.

# Semantics



- Referring to individuals
  - Jackie
  - son-of(Jackie), Sam
- Referring to states of the world
  - person(Jackie), female(Jackie)
  - mother(Sam, Jackie)

## FOL: Atomic sentences



AtomicSentence  $\rightarrow$  Predicate(Term, ...) | Term = Term

Term  $\rightarrow$  Function(Term, ...) | Constant | Variable

- Examples:
  - SchoolOf(Manos)
  - Colleague(TeacherOf(Alex), TeacherOf(Manos))
  - $>((+ x y), x)$

## FOL: Complex sentences

Sentence  $\rightarrow$  AtomicSentence  
| Sentence Connective Sentence  
| Quantifier Variable, ... Sentence  
|  $\neg$  Sentence  
| (Sentence)

- Examples:

- $S1 \wedge S2, S1 \vee S2, (S1 \wedge S2) \vee S3, S1 \Rightarrow S2, S1 \Leftrightarrow S3$
- $\text{Colleague}(\text{Paolo}, \text{Maja}) \Rightarrow \text{Colleague}(\text{Maja}, \text{Paolo})$   
 $\text{Student}(\text{Alex}, \text{Paolo}) \Rightarrow \text{Teacher}(\text{Paolo}, \text{Alex})$

## Semantics of atomic sentences

- Sentences in FOL are interpreted with respect to a **model**
- Model contains objects and relations among them
- Terms: refer to objects (e.g., Door, Alex, StudentOf(Paolo))
  - Constant symbols: refer to objects
  - Predicate symbols: refer to relations
  - Function symbols: refer to functional Relations
- An atomic sentence  $predicate(term_1, \dots, term_n)$  is **true** iff the relation referred to by  $predicate$  holds between the objects referred to by  $term_1, \dots, term_n$

## Example model

- **Objects:** John, James, Marry, Alex, Dan, Joe, Anne, Rich
- **Relation:** sets of tuples of objects  
{<John, James>, <Marry, Alex>, <Marry, James>, ...}  
{<Dan, Joe>, <Anne, Marry>, <Marry, Joe>, ...}
- E.g.:  
Parent relation -- {<John, James>, <Marry, Alex>, <Marry, James> }  
  
then **Parent(John, James)** is true  
**Parent(John, Marry)** is false

# Quantifiers



- Expressing sentences about **collections** of objects without enumeration (naming individuals)
- E.g., All Trojans are clever

Someone in the class is sleeping

- Universal quantification (for all):  $\forall$
- Existential quantification (there exists):  $\exists$

## Universal quantification (for all): $\forall$

$\forall$  *<variables>* *<sentence>*

- “Every one in the cs561 class is smart”:  
 $\forall x \text{ In}(cs561, x) \Rightarrow \text{Smart}(x)$
- **$\forall P$  corresponds to the conjunction of instantiations of  $P$**   
 $\text{In}(cs561, \text{Manos}) \Rightarrow \text{Smart}(\text{Manos}) \wedge$   
 $\text{In}(cs561, \text{Dan}) \Rightarrow \text{Smart}(\text{Dan}) \wedge$   
...  
 $\text{In}(cs561, \text{Clinton}) \Rightarrow \text{Smart}(\text{Clinton})$



## Universal quantification (for all): $\forall$



- $\Rightarrow$  is a natural connective to use with  $\forall$
- **Common mistake:** to use  $\wedge$  in conjunction with  $\forall$   
e.g:  $\forall x \text{ In}(cs561, x) \wedge \text{Smart}(x)$   
means *“every one is in cs561 and everyone is smart”*

## Existential quantification (there exists): $\exists$

$\exists$  *<variables>* *<sentence>*

- “Someone in the cs561 class is smart”:  
 $\exists x \text{ In}(\text{cs561}, x) \wedge \text{Smart}(x)$
- $\exists P$  corresponds to the disjunction of instantiations of P  
 $\text{In}(\text{cs561}, \text{Manos}) \wedge \text{Smart}(\text{Manos}) \vee$   
 $\text{In}(\text{cs561}, \text{Dan}) \wedge \text{Smart}(\text{Dan}) \vee$   
...  
 $\text{In}(\text{cs561}, \text{Clinton}) \wedge \text{Smart}(\text{Clinton})$

## Existential quantification (there exists): $\exists$



- $\wedge$  is a natural connective to use with  $\exists$
- **Common mistake:** to use  $\Rightarrow$  in conjunction with  $\exists$   
e.g:  $\exists x \text{ In}(cs561, x) \Rightarrow \text{Smart}(x)$   
is true if there is anyone that is not in cs561!  
(remember,  $\text{false} \Rightarrow \text{true}$  is valid).

## Properties of quantifiers

$\forall x \forall y$  is the same as  $\forall y \forall x$  (why??)

$\exists x \exists y$  is the same as  $\exists y \exists x$  (why??)

$\exists x \forall y$  is not the same as  $\forall y \exists x$

$\exists x \forall y \text{ Loves}(x, y)$

“There is a person who loves everyone in the world”

Not all by one  
person but  
each one at  
least by one

$\forall y \exists x \text{ Loves}(x, y)$

“Everyone in the world is loved by at least one person”

Quantifier duality: each can be expressed using the other

$\forall x \text{ Likes}(x, \text{IceCream}) \quad \neg \exists x \neg \text{Likes}(x, \text{IceCream})$  **Proof?**

$\exists x \text{ Likes}(x, \text{Broccoli}) \quad \neg \forall x \neg \text{Likes}(x, \text{Broccoli})$

## Proof

- In general we want to prove:

$$\forall x P(x) \iff \neg \exists x \neg P(x)$$

$$\square \forall x P(x) = \neg(\neg(\forall x P(x))) = \neg(\neg(P(x_1) \wedge P(x_2) \wedge \dots \wedge P(x_n))) = \neg(\neg P(x_1) \vee \neg P(x_2) \vee \dots \vee \neg P(x_n))$$

$$\square \exists x \neg P(x) = \neg P(x_1) \vee \neg P(x_2) \vee \dots \vee \neg P(x_n)$$

$$\square \neg \exists x \neg P(x) = \neg(\neg P(x_1) \vee \neg P(x_2) \vee \dots \vee \neg P(x_n))$$

## Example sentences



- Brothers are siblings
  -
- Sibling is transitive
  -
- One's mother is one's sibling's mother
  -
- A first cousin is a child of a parent's sibling
  -

## Example sentences

- Brothers are siblings

$$\forall x, y \text{ Brother}(x, y) \Rightarrow \text{Sibling}(x, y)$$

- Sibling is transitive

$$\forall x, y, z \text{ Sibling}(x, y) \wedge \text{Sibling}(y, z) \Rightarrow \text{Sibling}(x, z)$$

- One's mother is one's sibling's mother

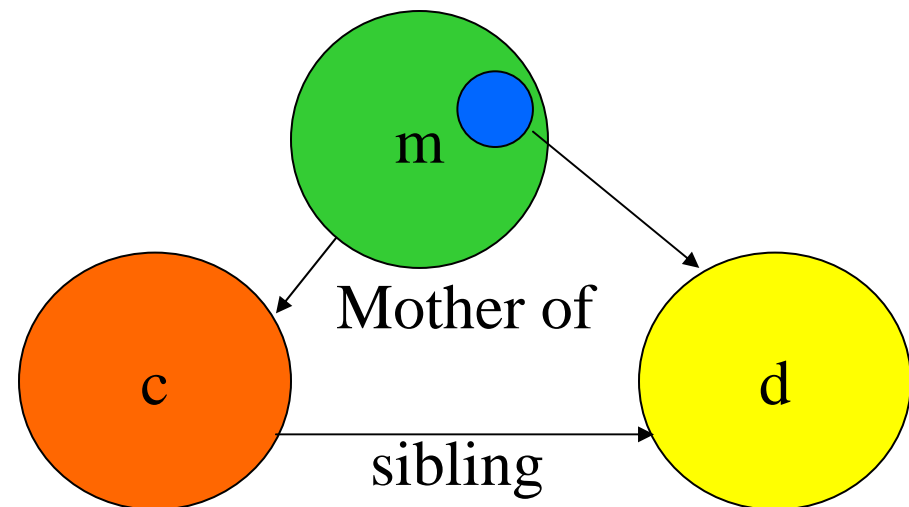
$$\forall m, c \text{ Mother}(m, c) \wedge \text{Sibling}(c, d) \Rightarrow \text{Mother}(m, d)$$

- A first cousin is a child of a parent's sibling

$$\forall c, d \text{ FirstCousin}(c, d) \Leftrightarrow \\ \exists p, ps \text{ Parent}(p, d) \wedge \text{Sibling}(p, ps) \wedge \text{Parent}(ps, c)$$

## Example sentences

- One's mother is one's sibling's mother  
 $\forall m, c, d \text{ Mother}(m, c) \wedge \text{Sibling}(c, d) \Rightarrow \text{Mother}(m, d)$
- $\forall c, d \exists m \text{ Mother}(m, c) \wedge \text{Sibling}(c, d) \Rightarrow \text{Mother}(m, d)$





# Translating English to FOL



- Every gardener likes the sun.

$\forall x \text{ gardener}(x) \Rightarrow \text{likes}(x, \text{Sun})$

- You can fool some of the people all of the time.

$\exists x \forall t (\text{person}(x) \wedge \text{time}(t)) \Rightarrow \text{can-fool}(x, t)$

## Translating English to FOL



- You can fool all of the people some of the time.

$$\forall \mathbf{x} \exists t (\text{person}(\mathbf{x}) \wedge \text{time}(t) \Rightarrow \text{can-fool}(\mathbf{x}, t))$$

- All purple mushrooms are poisonous.

$$\forall \mathbf{x} (\text{mushroom}(\mathbf{x}) \wedge \text{purple}(\mathbf{x})) \Rightarrow \text{poisonous}(\mathbf{x})$$

## Translating English to FOL...



- No purple mushroom is poisonous.

$\neg(\exists \mathbf{x}) \text{ purple}(\mathbf{x}) \wedge \text{mushroom}(\mathbf{x}) \wedge \text{poisonous}(\mathbf{x})$

or, equivalently,

$(\forall \mathbf{x}) (\text{mushroom}(\mathbf{x}) \wedge \text{purple}(\mathbf{x})) \Rightarrow \neg\text{poisonous}(\mathbf{x})$

## Translating English to FOL...

- There are exactly two purple mushrooms.

$$(\exists x)(\exists y) \text{ mushroom}(x) \wedge \text{purple}(x) \wedge \\ \text{mushroom}(y) \wedge \text{purple}(y) \wedge \neg(x=y) \wedge (\forall z) \\ (\text{mushroom}(z) \wedge \text{purple}(z)) \Rightarrow ((x=z) \vee (y=z))$$

- Deb is not tall.

$$\neg \text{tall}(\text{Deb})$$

## Translating English to FOL...

- X is above Y if X is on directly on top of Y or else there is a pile of one or more other objects directly on top of one another starting with X and ending with Y.

$$(\forall x)(\forall y) \text{above}(x,y) \iff (\text{on}(x,y) \vee (\exists z) (\text{on}(x,z) \wedge \text{above}(z,y)))$$

# Equality

$term_1 = term_2$  is true under a given interpretation  
if and only if  $term_1$  and  $term_2$  refer to the same object

E.g.,  $1 = 2$  and  $\forall x \times(Sqrt(x), Sqrt(x)) = x$  are satisfiable  
 $2 = 2$  is valid

E.g., definition of (full) *Sibling* in terms of *Parent*:

$$\forall x, y \text{ Sibling}(x, y) \Leftrightarrow [\neg(x = y) \wedge \exists m, f \neg(m = f) \wedge \\ \text{Parent}(m, x) \wedge \text{Parent}(f, x) \wedge \text{Parent}(m, y) \wedge \text{Parent}(f, y)]$$

## Higher-order logic?

- First-order logic allows us to quantify over objects (= the first-order entities that exist in the world).

- Higher-order logic also allows quantification over relations and functions.

e.g., “two objects are equal iff all properties applied to them are equivalent”:

$$\forall x,y \quad (x=y) \Leftrightarrow (\forall p, p(x) \Leftrightarrow p(y))$$

- Higher-order logics are more expressive than first-order; however, so far we have little understanding on how to effectively reason with sentences in higher-order logic. 39

# Logical agents for the Wumpus world

Remember: generic knowledge-based agent:

```
function KB-AGENT(percept) returns an action  
static: KB, a knowledge base  
         t, a counter, initially 0, indicating time  
TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))  
action ← ASK(KB, MAKE-ACTION-QUERY(t))  
TELL(KB, MAKE-ACTION-SENTENCE(action, t))  
t ← t + 1  
return action
```

1. TELL KB what was perceived  
Uses a KRL to insert new sentences, representations of facts, into KB
2. ASK KB what to do.  
Uses logical reasoning to examine actions and select best.



## Using the FOL Knowledge Base

Suppose a wumpus-world agent is using an FOL KB and perceives a smell and a breeze (but no glitter) at  $t = 5$ :

TELL( $KB$ ,  $Percept([Smell, Breeze, None], 5)$ )  
ASK( $KB$ ,  $\exists a \text{ Action}(a, 5)$ )

I.e., does the KB entail any particular actions at  $t = 5$ ?

Answer: *Yes*,  $\{a/Shoot\}$  ← substitution (binding list)  
Set of solutions

Given a sentence  $S$  and a substitution  $\sigma$ ,  
 $S\sigma$  denotes the result of plugging  $\sigma$  into  $S$ ; e.g.,  
 $S = Smarter(x, y)$   
 $\sigma = \{x/Hillary, y/Bill\}$   
 $S\sigma = Smarter(Hillary, Bill)$

ASK( $KB$ ,  $S$ ) returns some/all  $\sigma$  such that  $KB \models S\sigma$

## Wumpus world, FOL Knowledge Base

### “Perception”

$\forall b, g, t \text{ Percept}([Smell, b, g], t) \Rightarrow Smelt(t)$

$\forall s, b, t \text{ Percept}([s, b, Glitter], t) \Rightarrow AtGold(t)$

Reflex:  $\forall t \text{ AtGold}(t) \Rightarrow \text{Action}(Grab, t)$

Reflex with internal state: do we have the gold already?

$\forall t \text{ AtGold}(t) \wedge \neg \text{ Holding}(Gold, t) \Rightarrow \text{Action}(Grab, t)$

$\text{Holding}(Gold, t)$  cannot be observed

$\Rightarrow$  keeping track of change is essential

## Deducing hidden properties

Properties of locations:

$$\forall l, t \text{ At}(\text{Agent}, l, t) \wedge \text{Smelt}(t) \Rightarrow \text{Smelly}(l)$$

$$\forall l, t \text{ At}(\text{Agent}, l, t) \wedge \text{Breeze}(t) \Rightarrow \text{Breezy}(l)$$

Squares are breezy near a pit:

Diagnostic rule—infer cause from effect

$$\forall y \text{ Breezy}(y) \Rightarrow \exists x \text{ Pit}(x) \wedge \text{Adjacent}(x, y)$$

Causal rule—infer effect from cause

$$\forall x, y \text{ Pit}(x) \wedge \text{Adjacent}(x, y) \Rightarrow \text{Breezy}(y)$$

Neither of these is complete—e.g., the causal rule doesn't say whether squares far away from pits can be breezy

Definition for the *Breezy* predicate:

$$\forall y \text{ Breezy}(y) \Leftrightarrow [\exists x \text{ Pit}(x) \wedge \text{Adjacent}(x, y)]$$

# Situation calculus

Facts hold in situations, rather than eternally

E.g.,  $Holding(Gold, Now)$  rather than just  $Holding(Gold)$

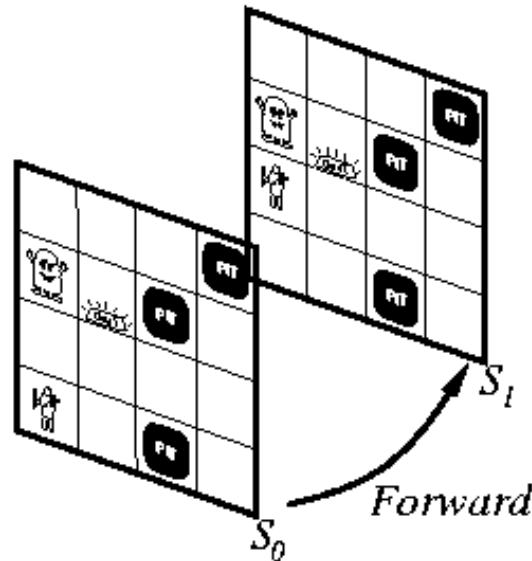
Situation calculus is one way to represent change in FOL:

    Adds a situation argument to each non-eternal predicate

    E.g.,  $Now$  in  $Holding(Gold, Now)$  denotes a situation

Situations are connected by the *Result* function

$Result(a, s)$  is the situation that results from doing  $a$  in  $s$



## Describing actions

“Effect” axiom—describe changes due to action

$$\forall s \text{ AtGold}(s) \Rightarrow \text{Holding}(\text{Gold}, \text{Result}(\text{Grab}, s))$$

“Frame” axiom—describe non-changes due to action

$$\forall s \text{ HaveArrow}(s) \Rightarrow \text{HaveArrow}(\text{Result}(\text{Grab}, s))$$

May result in  
too many  
frame axioms

Frame problem: find an elegant way to handle non-change

(a) representation—avoid frame axioms

(b) inference—avoid repeated “copy-overs” to keep track of state

Qualification problem: true descriptions of real actions require endless caveats—what if gold is slippery or nailed down or ...

Ramification problem: real actions have many secondary consequences—what about the dust on the gold, wear and tear on gloves, ...

## Describing actions (cont'd)

Successor-state axioms solve the representational frame problem

Each axiom is “about” a predicate (not an action per se):

P true afterwards  $\Leftrightarrow$  [an action made P true  
 $\vee$  P true already and no action made P false]

For holding the gold:

$$\forall a, s \text{ Holding}(\text{Gold}, \text{Result}(a, s)) \Leftrightarrow$$
$$[(a = \text{Grab} \wedge \text{AtGold}(s))$$
$$\vee (\text{Holding}(\text{Gold}, s) \wedge a \neq \text{Release})]$$

# Planning

Initial condition in KB:

$At(Agent, [1, 1], S_0)$

$At(Gold, [1, 2], S_0)$

Query:  $ASK(KB, \exists s \text{ Holding}(Gold, s))$

i.e., in what situation will I be holding the gold?

Answer:  $\{s / Result(Grab, Result(Forward, S_0))\}$

i.e., go forward and then grab the gold

This assumes that the agent is interested in plans starting at  $S_0$  and that  $S_0$  is the only situation described in the KB

## Generating action sequences

Represent plans as action sequences  $[a_1, a_2, \dots, a_n]$

$PlanResult(p, s)$  is the result of executing  $p$  in  $s$

Then the query  $ASK(KB, \exists p \text{ Holding}(Gold, PlanResult(p, S_0)))$   
has the solution  $\{p/[Forward, Grab]\}$

Definition of  $PlanResult$  in terms of  $Result$ :

$\forall s \text{ } PlanResult([], s) = s$  [ ] = empty plan

$\forall a, p, s \text{ } PlanResult([a|p], s) = PlanResult(p, Result(a, s))$

Recursively continue until it gets to empty plan [ ]

Planning systems are special-purpose reasoners designed to do this type of inference more efficiently than a general-purpose reasoner



# Summary



First-order logic:

- objects and relations are semantic primitives
- syntax: constants, functions, predicates, equality, quantifiers

Increased expressive power: sufficient to define wumpus world

Situation calculus:

- conventions for describing actions and change in FOL
- can formulate planning as inference on a situation calculus KB